

## ***List of topics – Basic Real Analysis Course***

**Preliminary Material. Topology Basics: Real numbers, set topology, metric spaces.**

### **Topology and continuous functions**

1. Baire category theorem
2. Urysohn theorem, extension theorem
3. Spaces of continuous functions, Stone-Weierstrass theorem, Arzela-Ascoli theorem

### **Measures and Measuring**

1. Sigma – Algebra of sets, Borel sigma-algebra
2. measurable functions
3. Monotone Class Lemmas
4. Measures, measure space, regular measure, signed measures
5. Fatou Lemma
6. Completion, extension and measure generation, Caratheodory theorem

### **III. Integration**

1. Definition and properties
2. Monotone convergence, Fatou lemma, Lebesgue's dominated convergence theorem, parameter dependence

### **IV. Spaces $L_p$**

1. Holder Inequality, Minkowski inequality
2. Riesz-Fischer Theorem
3. Density theorems

### **V. Convergence Types**

1. Convergence on measurement, near-anywhere convergence, near-uniform convergence, relations among them
2. Uniform Integrability

### **VI. Measure Decomposition**

1. Hahn decomposition and Jordan decomposition of signed measurements
2. Radon-Nikodym Theorem
3. Variables change
4. Lebesgue decomposition

## VII. Product Measurements

1. Fubini Theorem
2. Measurement Disintegration

## VII. Integral of Lebesgue-Stieltjes on $\mathbb{R}$

1. Lebesgue-Stieltjes Measurements
2. Absolutely continuous function
3. Function of limited variations
4. Fundamental theorem of calculus
5. Convolution

## Reference

Apostol, T.M.	Mathematical Analysis
Ash, R.B.	Real Analysis and Probability
Bartle, R.G.	The Elements of Real Analysis
Bartle, R.G.	The Elements of Integration
Cohn, D.L.	Measure Theory
Dudley, R.M.	Real Analysis and Probability
Dieudonné, J.	Foundations of Modern Analysis
Gelbaum, B., Olmsted, J.	Counterexamples in Analysis
Hewitt, E., Stromberg, K.	Real and Abstract Analysis
Kolmogorov, A., Fomin, S.	Elements in the Theory of Functions and
Functional Analysis	
Royden, H.	Real Analysis
Rudin, W.	Real and Complex Analysis
Stromberg, K.	Real Analysis
Taylor, A.E.	General Theory of Functions and Integration